

# Neural Networks Fall 2020

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## Exercise 1

Due date: November 2<sup>th</sup>

1. **(25 pts)** Given a set of samples  $D = \{(x_i, y_i)\}_{i=1 \text{ to } N}$ , we defined in class the problem of polynomial curve fitting as an error-minimization problem. Assuming that the labels  $\{y_i\}_{i=1}^N$  are i.i.d. and follow a Gaussian distribution whose mean is the prediction of the model  $h_w(x)$  of the curve-fitting problem,  $y_i \sim N(h_w(x_i), \sigma)$ , show that maximizing the logarithm of the likelihood function is equivalent to minimizing the square error function  $E(w) = \sum_{i=1 \text{ to } n} (h_w(x) - y_i)^2 / N$  we used in class. Recall that the likelihood is defined as  $L = p(D|w)$ .

2. **(25 pts)** We showed in class that for a zero-order polynomial (namely, a constant) the value that minimizes the squared error is the sample mean:  $h_w(x) = \sum_{i=1 \text{ to } N} y_i / N$ . Show that for the case of zero-order polynomial with an *absolute-value* error,  $E(w) = \sum_{i=1 \text{ to } N} |h_w(x) - y_i|$ , the optimal solution (the constant that minimizes the error) is the sample median.

3. **(25 pts)** The parity problem is defined as follows: given a set of  $k$  binary values (zeros and ones),

output 1 if there is an odd number of 1's, and  
output 0 otherwise.

a. Show that the perceptron algorithm discussed in class cannot learn to solve the parity

problem, (hint,  
use  $k=2$ ).

b. Write an algorithm that uses one memory cell and can solve the parity problem efficiently.